

2-23-15

5-4-1 Use Sum and Difference Identities

Ex1 Solve by rewriting the angle as a sum or difference

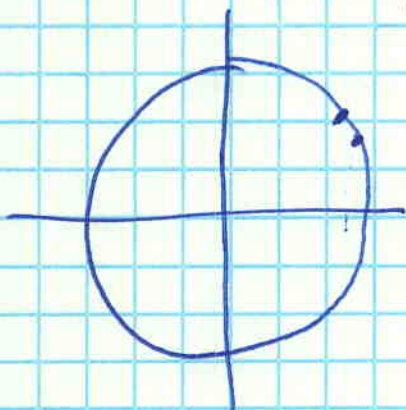
a) $\sin 15^\circ = \sin(\alpha - \beta)$

$\sin(\alpha - \beta) = \sin\alpha \cos\beta - \cos\alpha \sin\beta$

$= \sin 45^\circ \cos 30^\circ - \cos 45^\circ \sin 30^\circ$

$\left(\frac{\sqrt{2}}{2}\right)\left(\frac{\sqrt{3}}{2}\right) - \left(\frac{\sqrt{2}}{2}\right)\left(\frac{1}{2}\right)$

$\frac{\sqrt{6}}{4} - \frac{\sqrt{2}}{4}$ OR $\boxed{\frac{\sqrt{6} - \sqrt{2}}{4}}$



b) $\tan\left(\frac{7\pi}{12}\right) = \tan\left(\frac{3\pi}{12} + \frac{4\pi}{12}\right) = \tan\left(\frac{\pi}{4} + \frac{\pi}{3}\right)$

$\tan(\alpha + \beta) = \frac{\tan\alpha + \tan\beta}{1 - \tan\alpha \tan\beta} = \frac{\tan\frac{\pi}{4} + \tan\frac{\pi}{3}}{1 - \tan\frac{\pi}{4} \tan\frac{\pi}{3}}$

$\tan\frac{\pi}{4} = 1$ $\tan\frac{\pi}{3} = \sqrt{3}$
 ↑ (from Unit Circle) ↑

~~1 + \sqrt{3}~~ $\frac{1 + \sqrt{3}}{1 - \sqrt{3}}$

$\frac{(1 + \sqrt{3}) \cdot (1 + \sqrt{3})}{(1 - \sqrt{3}) \cdot (1 + \sqrt{3})} = \frac{1 + 2\sqrt{3} + 3}{1 - 3} = \frac{4 + 2\sqrt{3}}{-2}$

$\tan\frac{7\pi}{12} = \boxed{-2 - \sqrt{3}}$

* Separate angle into the sum or difference of known angles.

* Use sum/difference identities

EX 3 Reduce using the Sum or Difference Ident.

solve a) $\frac{\tan 32^\circ + \tan 13^\circ}{1 - \tan 32^\circ \tan 13^\circ}$ sum tangent angles

$$\tan(32^\circ + 13^\circ) = \boxed{\tan 45^\circ = 1}$$

b) $\sin x \sin 3x - \cos x \cos 3x$

$$-1(\cos x \cos 3x - \sin x \sin 3x)$$

cosine sum formula

$$(-1) \cos(x + 3x) = \boxed{-\cos 4x}$$

factor out -1
to switch
order

341: 1-3, 6, 11-13, 17-19, 72-73