

2.2 Day 2

Quadratic Form

$$Ax^2 + Bx + C$$

How can I get $Ax^6 + Bx^3 + C = 0$

Into a quadratic form?

$$\text{or } Ax^8 + Bx^4 + C = 0$$

$$x^8 = (x^4)^2$$

$$\text{or } Ax^{10} + Bx^5 + C = 0$$

$$x^{10} = (x^5)^2$$

$$\text{or } Ax^{20} + Bx^{10} + C = 0$$

$$x^{20} = (x^{10})^2$$

* Write $f(x)$ in terms of the "x" of the B term

$$A(x^4)^2 + Bx^4 + C = 0 \quad \text{or} \quad A(x^{10})^2 + Bx^{10} + C = 0$$

Substitute a simple variable for the more complicated one
 $x^n = u$

$$\text{EX: } x^4 - 8x^2 + 15 = 0$$

$$x^2 = u$$

$$u^2 - 8u + 15 = 0$$

sub "u" in for x^2

$$(u - 5)(u - 3) = 0$$

replace x^2

$$(x^2 - 5)(x^2 - 3) = 0$$

$$x^2 = 5 \quad ; \quad x^2 = 3$$

⋮

Zeros:

$f(x) = 0$ at the root "c"

$f(c) = 0$ $x=c$ is a solution ^(zero)

$(x-c)$ is a factor of $f(x)$

Repeated Zeros and Multiplicity

If $(x-c)$ is a repeated factor of $f(x)$, then c is a repeated zero.

The number of times a zero occurs is the multiplicity of that zero.

EX $(x-c)^3$, c has multiplicity 3

if odd multiplicity, then graph crosses x-axis

if even multiplicity, then graph tangent to x-axis

104- 25-27, 50-53, 64, 65, 86; 87, 112-113
Use "u"