

3.4 Log Application Problems

Pre-Calc

1. A population of polar bears in Canada can be modeled by the following equation: $y = 8000(.7)^x$ where y is the number of bears and x is the number of years that have elapsed. If the current equation remains consistent how long would it take for this population to become extinct?

$$1 = 8000(.7)^x$$

$$\frac{1}{8000} = .7^x$$

$$\log \frac{1}{8000} = \log .7^x$$

$$\log \frac{1}{8000} = x \log .7$$

$$x = \frac{\log \frac{1}{8000}}{\log .7}$$

$$x \approx 25.2 \text{ yr.}$$

Name: _____

2. If zombies are attacking (!) and the zombie population can be represented by the equation: $y = 2^x$ where y is the number of zombies and x is the number of days that have elapsed. How many days will it take for 1 million people to become zombies?

$$1,000,000 = 2^x$$

$$\log 1,000,000 = x \log 2$$

$$x = \frac{\log 1,000,000}{\log 2}$$

$$x \approx 19.93 \text{ yr.}$$

3. Kristi is deciding between several bank accounts. Each has a different interest rate and also calculates the interest accumulation in a different manner. She is going to deposit 300 dollars and the formulas for each bank are as follows: (Assume that she does not add or withdraw any funds and time is measured in years.)

Bank A uses the formula $A = 300 \left(1 + \frac{.08}{2}\right)^{2t}$

Bank C uses the formula $A = 300 \left(1 + \frac{.074}{365}\right)^{365t}$

Bank B uses the formula $A = 300 \left(1 + \frac{.075}{12}\right)^{12t}$

Bank D uses the formula $A = 300e^{.07t}$

I. How much money would each account have after 5 years?

A $A = 300 \left(1 + \frac{.08}{2}\right)^{2(5)}$

$A = 300 \left(1 + \frac{.08}{2}\right)^{10}$

$A = \$444.07$

D $A = 300e^{.07(5)}$

$A = \$425.72$

II. When she will have 600 dollars in each account?

A $600 = 300 \left(1 + \frac{.08}{2}\right)^{2t}$

$2 = \left(1 + \frac{.08}{2}\right)^{2t}$

$\log 2 = \log \left(1 + \frac{.08}{2}\right)^{2t}$

$\log 2 = 2t \cdot \log \left(1 + \frac{.08}{2}\right)$

$2 \log \left(1 + \frac{.08}{2}\right) \quad 2 \log \left(1 + \frac{.08}{2}\right)$

$t \approx 8.84 \text{ yr.}$

D $600 = 300e^{.07t}$

$2 = e^{.07t}$

$\ln 2 = \ln e^{.07t}$

$\ln 2 = .07t \ln e$

$\frac{\ln 2}{.07} = \frac{.07t \ln e}{.07} \quad \ln e = 1$

$9.9 \text{ yr.} \approx t$

III. Which account would you recommend to Kristi? Why?

3-4 Word Problem Practice

Exponential and Logarithmic Equations

1. **RADIOACTIVE DECAY** The amount of radium A present in a sample after t years can be modeled by $A = A_0 e^{-0.00043t}$, where A_0 is the initial amount. How long will it take 50 grams to decay to 10 grams?

$$10 = 50e^{-0.00043t}$$

3743 yr.

2. **BIOLOGY** Suppose a certain type of bacteria reproduces according to the model $P(t) = 100e^{0.271t}$, where t is time in hours and $P(t)$ is the number of bacteria.

a. Determine the growth rate.

$$27.1\%$$

b. What was the initial number of bacteria?

$$100$$

c. Find the number of bacteria in 5, 10, 24, and 72 hours. Round to the nearest whole number.

3. **RADIOACTIVITY** The amount of radioactivity in a sample is given by the equation $\ln(N) - \ln(N_0) = -kt$, where N is the current level, N_0 is the original level, k is the decay rate, and t is the time elapsed in hours. If the decay rate is 0.070, how many grams would be left after 24 hours if the original amount was 1000 grams?

$$\ln N - \ln 1000 = -0.070(24)$$

$$\ln \frac{n}{1000} = -1.68$$

$$e^{-1.68} = \frac{n}{1000}$$

$$1000 e^{-1.68} = n$$

186.4 grams

4. **INTEREST RATE** The effective annual yield E for an account that is compounded n times per year at r percent is given by the formula $E = \left[1 + \frac{r}{n}\right]^n - 1$. Suppose an account pays 5%. Use a calculator to find how many compounding periods it would take for the effective yield to be 5.1%.

$$17,288,942 \text{ Kw hr.}$$

5. If your precalculus teacher offers to give you 1 second of homework for the first week of school and double the amount of homework each week until the end of the school year (i.e. 2 seconds the second week), should you say yes? Explain.